



Kinetic modelling of the NO_x reduction by H₂ on Pt/WO₃/ZrO₂ catalyst in excess of O₂



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ABSTRACT

This paper addresses the elementary kinetic mean field modelling of the NO_x reduction by H₂ on Pt/WO₃/ZrO₂ under oxygen-rich conditions. Pt/WO₃/ZrO₂ was recently shown to reveal substantial low-temperature deNO_x activity with enhanced N₂ selectivity referred to traditional Pt catalysts. The model was developed based on a postulated reaction mechanism as well as kinetic examinations and implied a network of 48 reaction steps described by Arrhenius-based rate expressions. Kinetic parameters were taken from literature and by fitting calculations, while pre-exponential factors of adsorption were estimated from kinetic gas theory. For validation, experiments were simulated and thermodynamic consistency was proven by checking the Gibbs free enthalpy of the catalytic surface reactions. As a result of the kinetic model, the formation of OH surface species was identified as the rate determining step of H₂ oxidation, while the reduction of NO predominately occurs by dissociation of chemisorbed NO.

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1. Introduction

Anthropogenic pollutants such as carbon monoxide (CO), hydrocarbons (HC) and nitrogen oxides (NO_x) can cause persistent changes in the biosphere and are increasingly noticed with concern. Thus, an immense number of laws and regulations was remitted for the protection of the environment worldwide in the last decades. The most important origin of NO_x is the combustion of fossil energy sources like coal, natural gas, oil and fuel. In the combustion process, NO is the primary product oxidised, subsequently into NO₂ in atmospheric air. The preferred way to minimise the output of NO_x is the optimisation of the combustion process. Despite this, catalytic abatement technologies are more and more required to meet current and future legislation limits.

For the pollution control of gasoline cars, three way catalysts (TWC) comprising Pt/Rh or Pd/Rh are applied since the 1980s. TWC simultaneously abate NO_x, HC and CO and operate efficiently close to stoichiometric air/fuel ratio [1,2]. Although the reaction network of TWC is complex, the elementary processes are currently well understood [3]. Exemplarily, H₂ considerably contributes to NO_x reduction following the overall equation $2\text{NO} + 2\text{H}_2 \rightarrow \text{N}_2 + 2\text{H}_2\text{O}$.

In this concern, the NO–H₂ reaction was widely investigated for Pt, Pd and Rh catalysts, mostly in the absence of O₂ [4–6].

Furthermore, from oxygen-rich exhaust gases reflecting diesel engines, fossil power plants and waste combustion plants HC and CO can simply be removed by using Pt or Pd catalysts [1,7,8]. However, for the efficient reduction of NO_x, additional procedures are required. The classical lean deNO_x technique is the selective catalytic reduction by NH₃ (SCR) already introduced since the 1970s in fossil power plants. The most common SCR catalyst used today is V₂O₅/WO₃/TiO₂ [1,2,6,7], whereas for automotive exhaust Fe and Cu based zeolites are lately employed due to their advanced activity and thermal stability [9–13]. Additionally, in lean exhaust of passenger cars NO_x storage reduction catalysts (NSR) are also applied consisting of Pt, Pd and Rh as well as NO_x traps such as Al₂O₃, CeO₂ and BaCO₃. The operation of NSR is based on the periodic storage and reduction of NO_x [14,15]. The reduction is performed under rich conditions temporarily induced by engine management and is enhanced by the reaction of NO_x with H₂ on the precious metals components [16,17].

Moreover, the NO_x reduction by H₂ occurs effectively even in excess of O₂. A recent review reports considerable performance of precious metals [18], whereas Pt is highly active already at low temperatures (below 175 °C) being potentially relevant for automotive deNO_x [19]. SCR and NSR start operating above this temperature only. But as a constraint of lean H₂–deNO_x, the hydrogen mainly reacts with the excessive O₂ resulting in low

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H₂ selectivity towards NO_x reduction. Another issue is the pronounced production of N₂O on most Pt, Ir, Rh and Pd catalysts [16]. However, Pt/La_{0.7}Sr_{0.2}Ce_{0.1}FeO₃ [20,21] and Pt/MgO–CeO₂ [22–24] were lately demonstrated to reveal substantially increased selectivity of N₂. Additionally, we reported on Pt/WO₃/ZrO₂ showing marked lean H₂–deNO_x between 50 and 450 °C and high N₂ selectivity up to 90% [25]. For comparison, classical Pt/Al₂O₃ performs only from 50 to 150 °C with a N₂O selectivity of about 80%. Pt/WO₃/ZrO₂ also implies outstanding hydrothermal stability as well as resistance against SO_x. Related Pd/WO₃/ZrO₂ catalysts even show selective formation of N₂, but their activity is limited to a narrow operation window [26]. High activity and N₂ selectivity are also evidenced for LaCoO₃–supported Pd [27], while an enhancing effect of H₂ is highlighted for NO_x reduction by hydrocarbons (lean HC–SCR) using Ag/Al₂O₃ catalysts [28–30].

In situ, spectroscopic studies of the H₂–O₂–NO_x reaction on Pt/WO₃/ZrO₂ [25] suggest that the conversion is in accordance with the mechanism widely accepted for Pt catalysts [3,16,31]. This pathway involves the adsorption of NO on reduced Pt sites followed by dissociation into chemisorbed N and O atoms. The recombination of two adjacent N species finally leads to N₂, whereas N₂O is produced by reaction of an N atom with NO both adsorbed on neighbouring Pt sites. NO_x surface species formed on the support are not supposed to be predominately involved in lean H₂–deNO_x on Pt/WO₃/ZrO₂. Such a mechanism is proposed for Pt/La_{0.7}Sr_{0.2}Ce_{0.1}FeO₃ [21] and Pt/MgO–CeO₂ [22].

The objective of this paper is to advance the understanding of the lean H₂–O₂–NO_x reaction on Pt/WO₃/ZrO₂. For this purpose, we performed kinetic investigations to construct a kinetic mean field model based on elementary reactions. Finally, the kinetic model was validated by comparing experiments and predictions as well as checking thermodynamic consistency of the kinetic parameters modelled.

2. Experimental

2.1. Preparation and characterisation of the catalyst

The preparation and characterisation of the Pt/WO₃/ZrO₂ catalyst were reported recently. Thus, only a brief description is given here [25]. The tetragonal ZrO₂ substrate was obtained by hydrazine synthesis with final calcination in air at 750 °C for 6 h. The introduction of WO₃ and Pt was successively performed by using the incipient wetness impregnation method. The ZrO₂ substrate was treated with an aqueous solution of (NH₄)₆H₂W₁₂O₄₁ (Fluka), and after overnight drying Pt was added by taking an aqueous Pt(NO₃)₂ solution (Chempur). The sample was activated at 300 °C in a flowing mixture of 9 vol% H₂ and 91 vol% N₂ and was finally conditioned in static air at 500 °C for 5 h. The content of Pt amounted to 0.3%, whereas that of W was 11% both referring to bare ZrO₂ carrier. The BET surface area of Pt/WO₃/ZrO₂ was about 70 m²/g. Pt revealed a dispersion of 90%, while WO₃ existed in the form of nano-scaled particles as well as larger amorphous entities [25].

For the kinetic studies, a commercial cordierite honeycomb with a cell density of 400 cpsi was coated with the catalyst at Umicore company (Hanau). The resulting load of Pt/WO₃/ZrO₂ amounted to 100 g/l.

2.2. Kinetic studies

Kinetic studies were performed by using a gradient-free loop reactor with external gas cycle (MZZC pump, Vacuubrand) [32]. The measurements were made by using a cylindrical core (*d* = 10 mm, *l* = 5 mm) taken from the coated monolith. The honeycomb was packed into the quartz glass tube of the reactor, fixed with quartz

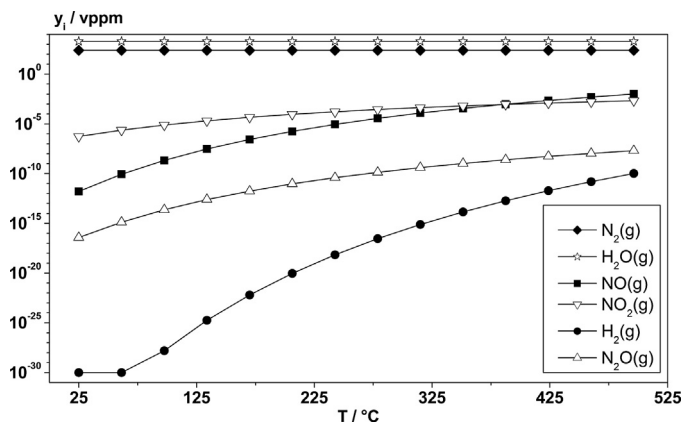


Fig. 1. Equilibrium composition of the H₂–O₂–NO_x reaction; reaction mixture: *y*(NO) = 500 vppm, *y*(H₂) = 2000 vppm, *y*(O₂) = 5 vol%, Ar balance.

wool and then the feed was added. The total volumetric flow (*F*) was 500 ml/min (STP) with a recycle ratio ψ ($\psi = F_{\text{loop}}/F_{\text{out}}$) of 80. The gas hourly space velocity (GHSV) was 77,000 h^{−1}. As checked by tracer experiments, the residence time behaviour of the reactor corresponded well to that of a continuous stirred tank reactor (CSTR).

The feed was a blend of pure components (Air Liquide) dosed from independent flow controllers (Bronkhorst) and consisted of H₂, O₂ and NO balanced by N₂. Additionally, some measurements were also made in the absence of NO to study the kinetics of the H₂–O₂ reaction independently. The temperature was monitored by two K-type thermocouples located directly in front of and behind the honeycomb. The maximum difference of inlet and outlet temperature was found to be 8 K. The simultaneous analyses of NO, NO₂, N₂O, NH₃, and H₂O was carried out by a hot measuring FTIR spectrometer (MULTI-GAS Analyzer 2030, MKS Instruments). O₂ was monitored by a lambda probe (LSU 4.9, Bosch). The reactor effluents were recorded after reaching steady state; no oscillating behaviour of the Pt/WO₃/ZrO₂ catalyst was found in all experiments [33].

3. Results and discussion

3.1. Thermodynamics of the H₂–O₂–NO_x reaction

The thermodynamics of the lean H₂–deNO_x reaction were calculated by HSC Thermodynamic Software 5.1 from Outokumpu. The results are exemplarily shown in Fig. 1 for a reaction mixture composed of 500 vppm NO, 2000 vppm H₂ and 5 vol% O₂ balanced by Ar implying the chemical equilibrium of NO, NO₂, N₂O, N₂, O₂, H₂ and H₂O. The equilibrium composition evidences that N₂ and H₂O are clearly the favoured products, whereas N₂O is only present in negligible amounts.

3.2. Kinetic modelling

For the construction of the kinetic model of lean H₂–deNO_x we followed a stepwise approach. In the first step, the catalytic reaction of H₂ with O₂ was separately investigated. This was done to reduce the number of free parameters in the numeric modelling and to study the kinetics independently, since the H₂ oxidation is significantly affected by the presence of NO as will be shown in Section 3.2.3. In the second step, the NO_x reduction was implemented into the model of the H₂–O₂ reaction including the formation of N₂ and N₂O. The conversions are described by a set of elementary reactions implying forward and backward reactions (Eqs. (1)–(6) and (31)–(35)). In these reaction equations, the free Pt sites considered as the catalytically active sites [3,16,25,32,34] are labelled

by an asterisk (*). Furthermore, the mean field approximation is employed supposing equivalence of the active Pt sites [3,7,34].

Limitation of the catalytic conversions by film and pore diffusion are excluded by checking Mears Weisz Prater criterion [35], and analysing Arrhenius plots.

3.2.1. Kinetic modelling of the H₂–O₂ reaction

The kinetic model of the H₂ oxidation on Pt/WO₃/ZrO₂ is expressed by Eqs. (1)–(6) implying 4 surface species, 3 gas-phase species and 6 reaction steps according to the literature [34,36–38]. This model includes the dissociative adsorption and desorption of H₂ (Eq. (1)) and O₂ (Eq. (2)) as well as the molecular adsorption and desorption of H₂O (Eq. (6)). Additionally, two parallel routes of catalytic H₂O formation are considered including the combination of OH and H and the reaction of OH surface species (Eqs. (3)–(5)). Gas-phase reactions do not play a role under the present reaction conditions as checked by preliminary experiments.



For every reaction, an Arrhenius-based rate expression is used (Eqs. (7)–(18)), where A_i is the pre-exponential factor and E_i the activation energy. It should be pointed out that for H₂ adsorption (Eq. (7)), the reaction order of Θ_* is assumed to be unity due to very fast diffusion of H and H₂, reducing the effect of the number of unoccupied Pt sites on the adsorption rate [34]. Furthermore, $E_2(0)$ and $E_4(0)$ are the activation energies for desorption of H₂ and O₂ at zero coverage, while the respective correction factor α_i implies linear dependency of $E_i(0)$ on the coverage (θ_i) due to repulsive interactions of the surface species [39–42].

$$r_1 = A_1 \exp\left(-\frac{E_1}{RT}\right) c_{\text{H}_2} \Theta_* \quad (7)$$

$$r_2 = A_2 \exp\left(-\frac{E_2(0) - \alpha_2 \Theta_{\text{H}}}{RT}\right) \Theta_{\text{H}}^2 \quad (8)$$

$$r_3 = A_3 \exp\left(-\frac{E_3}{RT}\right) c_{\text{O}_2} \Theta_*^2 \quad (9)$$

$$r_4 = A_4 \exp\left(-\frac{E_4(0) - \alpha_4 \Theta_{\text{O}}}{RT}\right) \Theta_{\text{O}}^2 \quad (10)$$

$$r_5 = A_5 \exp\left(-\frac{E_5}{RT}\right) \Theta_{\text{O}} \Theta_{\text{H}} \quad (11)$$

$$r_6 = A_6 \exp\left(-\frac{E_6}{RT}\right) \Theta_{\text{OH}} \Theta_* \quad (12)$$

$$r_7 = A_7 \exp\left(-\frac{E_7}{RT}\right) \Theta_{\text{OH}} \Theta_{\text{H}} \quad (13)$$

$$r_8 = A_8 \exp\left(-\frac{E_8}{RT}\right) \Theta_{\text{H}_2\text{O}} \Theta_* \quad (14)$$

$$r_9 = A_9 \exp\left(-\frac{E_9}{RT}\right) \Theta_{\text{OH}}^2 \quad (15)$$

$$r_{10} = A_{10} \exp\left(-\frac{E_{10}}{RT}\right) \Theta_{\text{H}_2\text{O}} \Theta_{\text{O}} \quad (16)$$

$$r_{11} = A_{11} \exp\left(-\frac{E_{11}}{RT}\right) \Theta_{\text{H}_2\text{O}} \quad (17)$$

$$r_{12} = A_{12} \exp\left(-\frac{E_{12}}{RT}\right) c_{\text{H}_2\text{O}} \Theta_* \quad (18)$$

The numeric modelling is based on the stationary CSTR mass balance accounting for the gas-phase (Eq. (19)) and adsorbed species (Eq. (20)). v_{ij} denotes the respective stoichiometric coefficient, A_{act} the active Pt surface and Γ the surface concentration of active sites ($\Gamma = 2.05 \times 10^{-5} \text{ mol m}^{-2}$ [43,44]), which was simply derived from Pt dispersion, the amount of Pt and the catalyst surface area.

$$\frac{dc_i}{dt} = 0 = F \times (c_{i,\text{in}} - c_{i,\text{out}}) + A_{\text{act}} \times \sum_{\substack{i=1 \\ i \neq j}}^n v_{ij} r_j \quad (19)$$

$$\frac{d\Theta_i}{dt} = 0 = \frac{1}{\Gamma} \times \sum_{\substack{i=1 \\ i \neq j}}^n v_{ij} r_j \quad (20)$$

To reduce the number of free parameters in the fitting procedure, some kinetic parameters are adopted from the literature, while the pre-exponential factors of the adsorption of H₂ (A_1) and O₂ (A_3) are estimated based on the kinetic gas theory (Eq. (21)); N_A is the Avogadro number, R the molar gas constant, M_i the molar mass of the gas species, a_m the surface area per Pt site ($a_m = 6.03 \times 10^{-20} \text{ m}^2 \text{ site}^{-1}$) calculated from the atomic radius of Pt ($r_a = 1.385 \times 10^{-10} \text{ m}$ [45]) and S^0 is the sticking coefficient for zero coverage [44,46]. The sticking coefficients are taken from the literature; for O₂ S^0 is 0.07, for H₂ 0.046 and for H₂O it is 0.75 [34,43,46]. In the calculations, the temperature dependency of A_i is neglected, i.e. A_i is determined for 70 °C representing a mean temperature in the kinetic studies.

$$A_i = \frac{N_A RT}{(2\pi M_i RT)^{1/2}} a_m \Gamma S^0 \quad (21)$$

Furthermore, the adsorption steps are assumed to occur non-activated, i.e. $E_1 = E_3 = E_{12} = 0 \text{ kJ mol}^{-1}$ being in good agreement with the literature [34,47]. The kinetic parameters for desorption of O₂ (A_4 , $E_4(0)$, α_4) are elucidated from kinetic reinvestigation of the pattern of the temperature programmed O₂ desorption on Pt/WO₃/ZrO₂ taken from our previous paper [25] providing slightly different kinetic parameters only. Furthermore, $E_2(0)$ and α_2 are adopted from related Pt catalysts [34], while the kinetic parameters of the backward reactions of Eqs. (3)–(5) (A_6 , E_6 , A_8 , E_8 , A_{10} and E_{10}) as well as the activation energy for water desorption (E_{11}) is calculated from the thermodynamic equilibrium using NASA polynomials [34,48]. Finally, the remaining parameters, A_2 , A_5 , A_7 , A_9 , A_{11} , E_5 , E_7 and E_9 are numerically fitted using the Matlab tool Isqcurvefit (nonlinear regression). The temperature depending surface coverages are calculated with the Matlab solver ode15s. For the fits, two sets of experimental data are simultaneously taken referring to different feed compositions ($y(\text{H}_2) = 2300 \text{ vppm}$,

Table 1
Kinetic parameters of the model of the H₂–O₂ reaction on Pt/WO₃/ZrO₂.

Parameter	Value	Tolerance ^a	Unit	Reference
A ₁	16.1		[m s ⁻¹]	Calculated ^b
E ₁	0		[kJ mol ⁻¹]	[34]
A ₂	4.0 × 10 ¹¹		[mol (m ² s) ⁻¹]	Numerical fit
E ₂ (0)	69.11		[kJ mol ⁻¹]	[34]
α ₂	6		[kJ mol ⁻¹]	[34]
A ₃	8.1		[m s ⁻¹]	Calculated ^b
E ₃	0		[kJ mol ⁻¹]	[34]
A ₄	1.2 × 10 ¹⁰	±1.0 × 10 ¹⁰	[mol (m ² s) ⁻¹]	Numerical fit
E ₄ (0)	182.6	±5.6	[kJ mol ⁻¹]	Numerical fit
α ₄	61.9	±3.5	[kJ mol ⁻¹]	Numerical fit
A ₅	1.2 × 10 ¹¹		[mol (m ² s) ⁻¹]	Numerical fit
E ₅	84		[kJ mol ⁻¹]	Numerical fit
A ₆	3.2 × 10 ¹¹		[mol (m ² s) ⁻¹]	Calculated ^c
E ₆	144.1		[kJ mol ⁻¹]	Calculated ^c
A ₇	7.4 × 10 ¹⁴		[mol (m ² s) ⁻¹]	Numerical fit
E ₇	56.4		[kJ mol ⁻¹]	Numerical fit
A ₈	1.3 × 10 ¹⁴		[mol (m ² s) ⁻¹]	Calculated ^c
E ₈	106.5		[kJ mol ⁻¹]	Calculated ^c
A ₉	1.8 × 10 ⁴		[mol (m ² s) ⁻¹]	Numerical fit
E ₉	57.4		[kJ mol ⁻¹]	Numerical fit
A ₁₀	1.2 × 10 ⁴		[mol (m ² s) ⁻¹]	Calculated ^c
E ₁₀	47.3		[kJ mol ⁻¹]	Calculated ^c
A ₁₁	8.6 × 10 ¹²		[mol (m ² s) ⁻¹]	Numerical fit
E ₁₁	40.8		[kJ mol ⁻¹]	Calculated ^c
A ₁₂	87.3		[m s ⁻¹]	Calculated ^b
E ₁₂	0		[kJ mol ⁻¹]	[34]

^a 95% confidence interval.

^b Calculated with Eq. (21).

^c Calculated from thermodynamic constraints.

y(O₂) = 3 vol% and y(H₂) = 2300 vppm, y(O₂) = 4 vol%). Since the fitting procedure is carried out based on 8 experimental data points, the 95% confidence interval is not meaningful to assess the accuracy of the kinetic parameters calculated. Thus, the corresponding R²

parameters ($R^2 = 1 - \sum_{i=1}^n (y_{i,\text{exp}} - y_{i,\text{model}})^2 / (y_{i,\text{exp}} - \bar{y}_{\text{exp}})^2$) are

taken.

Fig. 2 evidences that the experimental H₂O content is well described by the model and the kinetic parameters implemented therein (Table 1). The accuracy of the fitting is reflected by the high R² parameters being close to 1. Furthermore, the simulated surface coverage (Fig. 3) indicated chemisorbed O to be the prevailing surface species with minor abundance of H*. The remaining species are present in negligible surface concentrations, which is in line with the literature [34,44]. The calculated activation energy of O₂ desorption at zero coverage (E₄(0) = 182.6 kJ mol⁻¹) is close to that of Pt catalysts reported in the literature, i.e. 200 kJ mol⁻¹ [41] and 213 kJ mol⁻¹ [49], respectively. The determined activation energy for H₂O desorption (E₁₁ = 40.8 kJ mol⁻¹) is also close to literature data. Deutschmann et al. specifies values of 40.3 kJ mol⁻¹ [34] and 49.2 kJ mol⁻¹ [47]. Warnatz et al. reported a slightly higher activation energy for desorption of water (62.8 kJ mol⁻¹) [37]. The fitted values of the activation energies for the surface reactions shown in Eqs. (3)–(5) (E₅–E₁₀) are higher than corresponding data reported for the H₂ oxidation on Pt catalysts. The activation energy for the formation of OH surface groups by Eq. (3) (E₅) is shown to be 70 kJ mol⁻¹ [47] and 11.5 kJ mol⁻¹ [34] (this work: 84 kJ mol⁻¹). E₇ is specified with 17.4 kJ mol⁻¹ (this work: 56.4 kJ mol⁻¹) and E₉ with 48.2 kJ mol⁻¹ (this work: 57.4 kJ mol⁻¹), respectively [34,47]. It may be noticed, that the different activation energies of model and literature are attributed to the different composition of the catalysts and are considered to be reasonable due to specific interaction of Pt with respective substrate. For example, the data of Deutschmann et al. are referred to a polycrystalline Pt foil [34,38], while that from Koop et al. are associated with Pt/γ-Al₂O₃ cata-

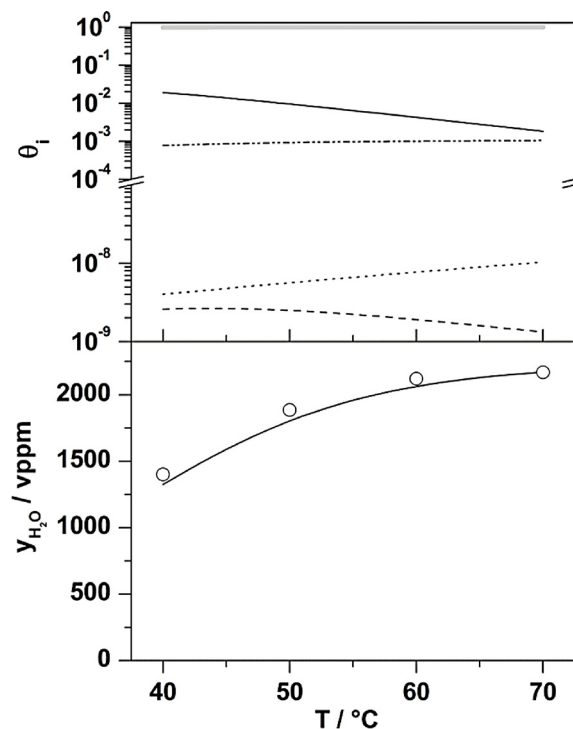


Fig. 6. Experimental (○) and simulated H₂O fraction (—, R² = 0.96) as well as simulated coverages of Pt/WO₃/ZrO₂ by O* (---), H* (···), OH* (- · - ·), H₂O* (—) and vacant Pt sites (— · —) in H₂ oxidation. Conditions: y(H₂) = 2300 vppm, y(O₂) = 6 vol%, balance N₂, GHSV = 77,000 h⁻¹.

lysts [47]. Additionally, also some effect might also be assigned to the different size of the Pt particles as discussed in Section 3.2.4.

Furthermore, from the kinetic analysis, it is deduced that the dissociative adsorption of O₂ (Eq. (2)) is the rate determining step of the H₂ oxidation on Pt/WO₃/ZrO₂. This conclusion is in line with the literature addressing traditional Pt catalysts [34]. The kinetic model also evidences that adsorbed water is preferentially produced by the reaction of OH* with H* (Eq. (4)), whereas the competitive route by two OH* species contributes to minor extent only (Eq. (5)).

3.2.2. Validation of the kinetic model of the H₂–O₂ reaction

For validation of the kinetic model, the remaining kinetic measurements are simulated implying O₂ variation from 0.5 to 5 vol%. The simulations are performed based on Eqs. (19) and (20) using the respective experimental conditions as well as the kinetic parameters presented in Table 1. Figs. 4–6 show that the experimental H₂O formation is well described by the simulations as demonstrated by the high R² parameters. The maximum difference between experimental and calculated data amounts to 5% only. Furthermore, the kinetic model shows that regardless of the feed content of O₂ the Pt sites are mainly covered by O*, while other surface groups (H*, OH* and H₂O*) are present in little quantity. It is also worth noting that unoccupied Pt sites are still available, although the temperatures are rather low potentially favouring adsorption processes.

For further validation, the thermodynamic consistency of the kinetic parameters implemented into the elementary kinetic model is also evaluated [50]. Calorimetric studies from Yeo et al. indicate that at 20 °C the enthalpy of the dissociative chemisorption of O₂ on Pt(111) lies in the range of about –125 kJ mol⁻¹ at steady state [51], whereas another value is reported to be –219 kJ mol⁻¹ [34]. With the kinetic model, the adsorption enthalpy is calculated as ΔH_{ads} = E₃ – E₄(0) = –182.6 kJ mol⁻¹ lying in the broad range of above literature data. Furthermore, for the catalytic H₂ oxidation, the reaction enthalpy and reaction entropy are deduced

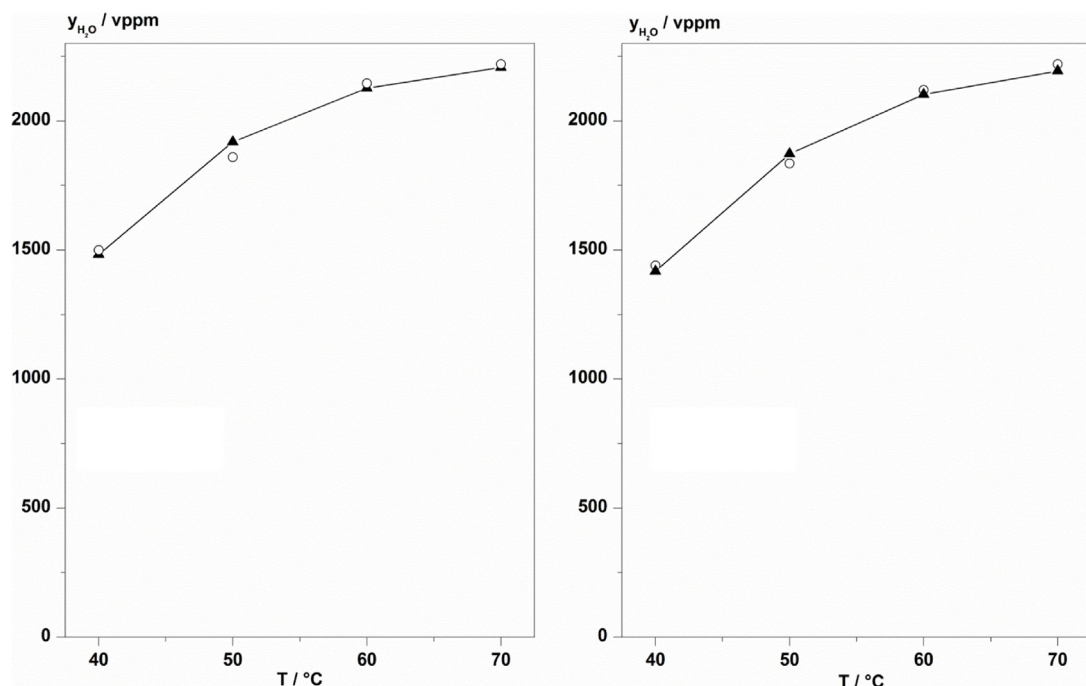


Fig. 2. Experimental (○) and fitted H_2O fraction (—▲—) in H_2 oxidation on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ with O_2 fraction of 3 vol% (left, $R^2 = 0.99$) and 4 vol% (right, $R^2 = 0.99$); lines are guides for the eyes. Conditions: $y(\text{H}_2) = 2300$ vppm, balance N_2 , GHSV = 77,000 h^{-1} .

from Eqs. (22) and (23), respectively, where c_{ij} are factors of linearly decomposed reactions. These coefficients are determined by row echelon reduction of the reaction mechanism [50] following similar calculations presented in [52] expressing the sequence of elementary and linearly independent reactions occurring in the formation of gaseous H_2O . From these mathematical operations, Eq. (24) is obtained for the enthalpy ($\Delta_R H_S$) and Eq. (25) for the

entropy ($\Delta_R S_S$) of the catalytic surface reactions. It should be noted that Eq. (5) is a linearly dependent reaction; and is therefore, not considered for the enthalpy and entropy calculations. This approach results in an enthalpy of $\Delta_R H_S = -241.9 \text{ kJ mol}^{-1}$ being very close to that determined for the enthalpy (Eqs. (26) and (27)) for the gas-phase reaction $\text{H}_2(\text{g}) + 0.5 \text{O}_2(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g})$ at 70 °C, i.e. $\Delta_R H_g(T = 70^\circ\text{C}) = -242.5 \text{ kJ mol}^{-1}$. The thermo-chemical data used

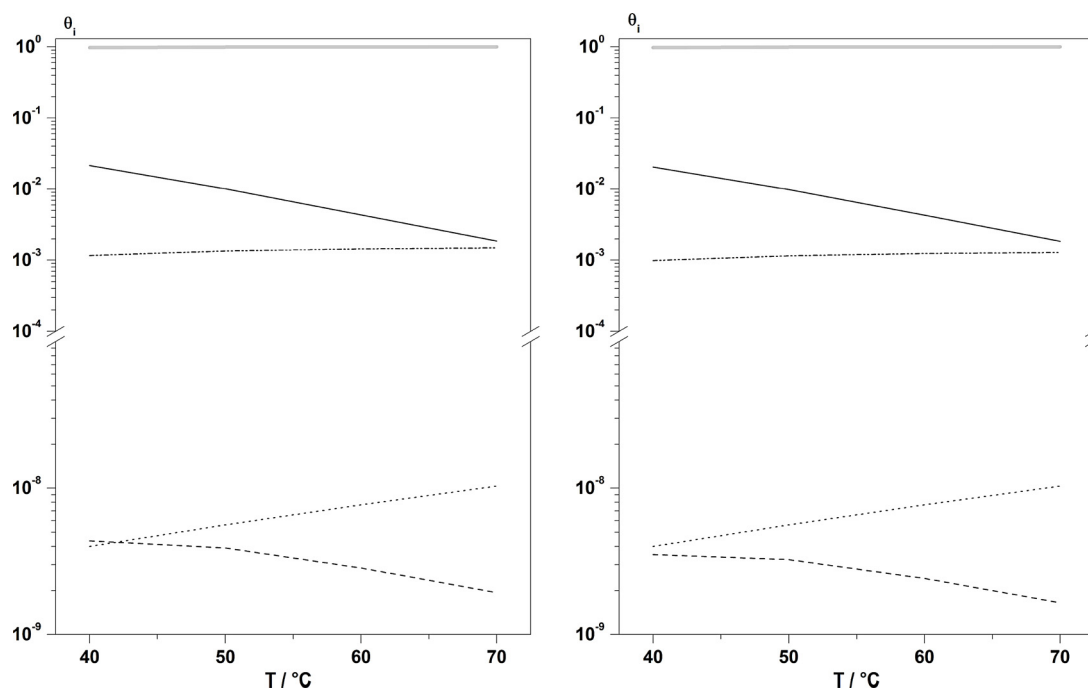


Fig. 3. Simulated coverages of $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ by O^* (—), H^* (---), OH^* (···), H_2O^* (— · —) and vacant Pt sites (— · — · —) in H_2 oxidation with O_2 fraction of 3 vol% (left) and 4 vol% (right). Corresponding gas-phase fractions and conditions are demonstrated in Fig. 2.

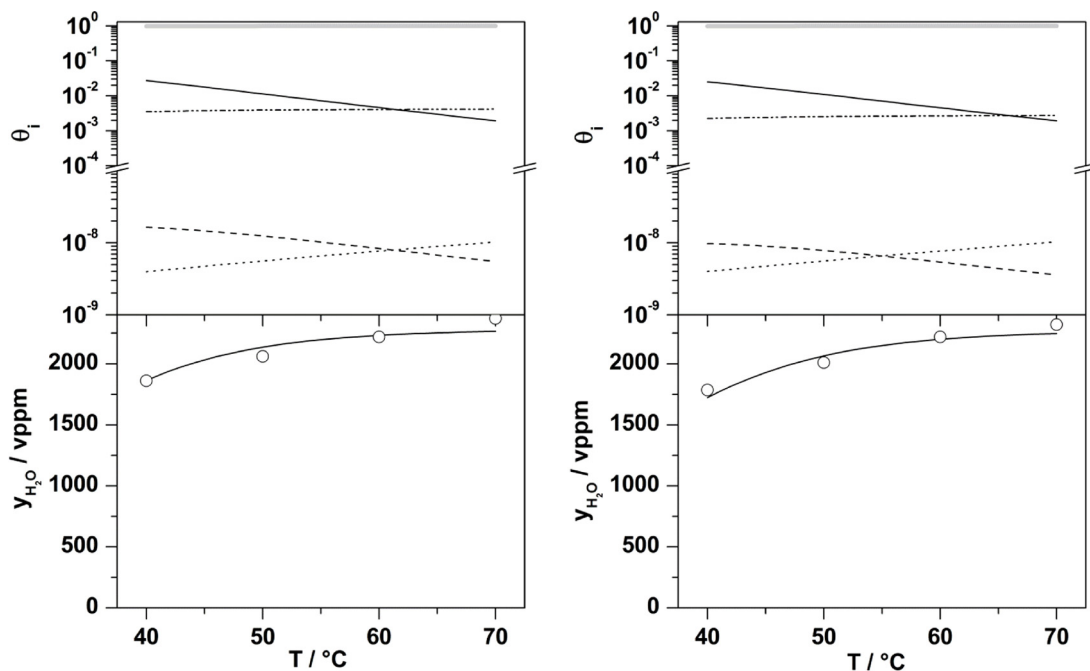


Fig. 4. Experimental (○) and simulated H₂O fraction (—) as well as simulated coverages by O* (—), H* (—), OH* (···), H₂O* (—) and vacant Pt sites (---) in H₂ oxidation on Pt/WO₃/ZrO₂ with O₂ fraction of 0.5 vol% (left, R² = 0.88) and 1 vol% (right, R² = 0.93). Conditions: y(H₂) = 2300 vppm, balance N₂, GHSV = 77,000 h⁻¹.

for the calculation of $\Delta_R H_g$ (Eqs. (26) and (27)) are taken from the literature [53].

$$\Delta_R H_s = \sum_{i=1}^n \sum_{j=1}^n c_{ij} (E_j^f - E_j^b) \quad (22)$$

$$\Delta_R S_s = R \ln \prod_{i=1}^n \left(\frac{A_i^f}{A_i^b} \right)^{c_{ij}} \quad (23)$$

$$\Delta_R H_s = (E_1 - E_2(0)) + 0.5(E_3 - E_4(0)) + (E_5 - E_6) + (E_7 - E_8) + (E_{11} - E_{12}) \quad (24)$$

$$\Delta_R S_s = R \ln \left(\frac{A_1}{A_2} \left(\frac{A_3}{A_4} \right)^{0.5} \frac{A_5}{A_6} \frac{A_7}{A_8} \frac{A_{11}}{A_{12}} \right) \quad (25)$$

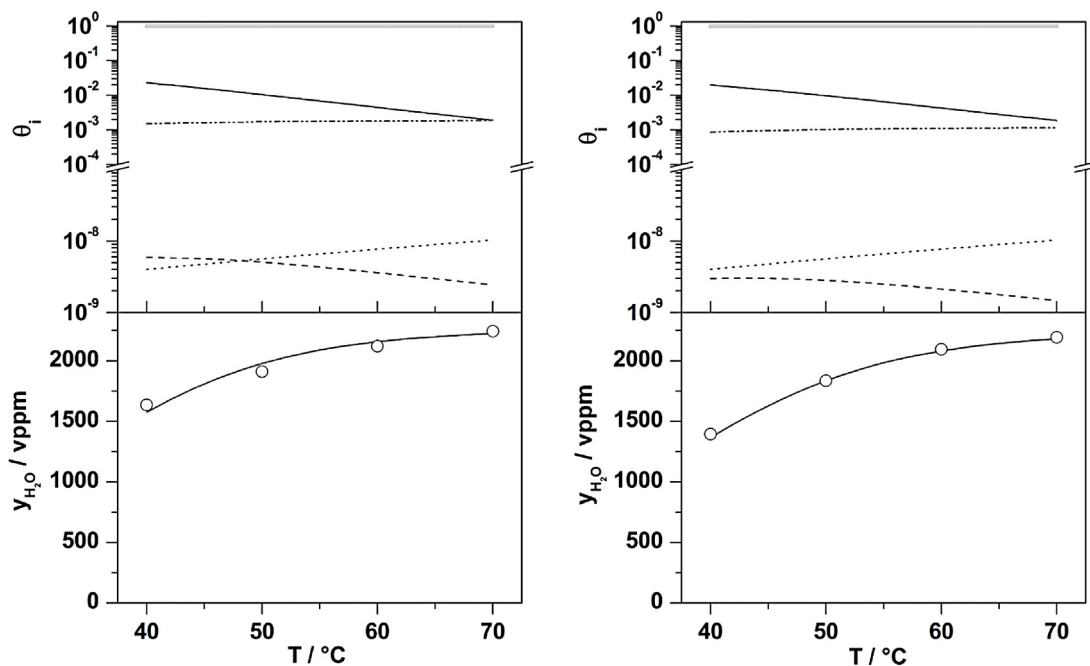


Fig. 5. Experimental (○) and simulated H₂O fraction (—) as well as simulated coverages of Pt/WO₃/ZrO₂ by O* (—), H* (—), OH* (···), H₂O* (—) and vacant Pt sites (---) in H₂ oxidation with O₂ fraction of 2 vol% (left, R² = 0.95) and 5 vol% (R² = 0.99). Conditions: y(H₂) = 2300 vppm, balance N₂, GHSV = 77,000 h⁻¹.

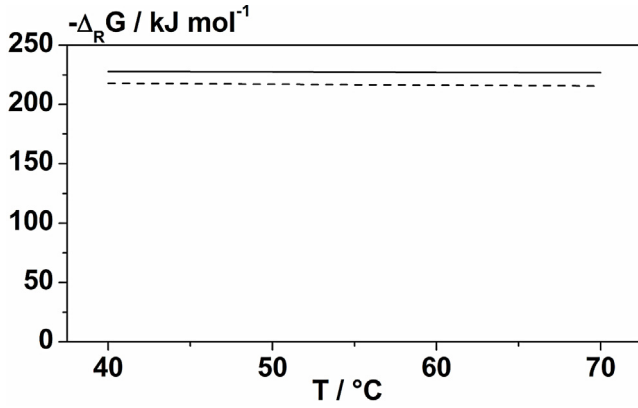


Fig. 7. Gibbs free enthalpy of the H_2 oxidation ($\text{H}_2(\text{g}) + 0.5 \text{O}_2(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g})$) calculated with thermochemical data (—) and kinetic parameters of the surface reaction on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ (---).

$$\Delta_R H_g(T) = \sum_{\substack{i=1 \\ i \neq j}}^n \nu_{ij} H_{g,i}(T) \quad (26)$$

$$H_{g,i}(T) = H_{g,i}(T_0) + \int_{T_0}^T c_{p,i} dT \quad (27)$$

From the kinetic parameters, a reaction entropy of $\Delta_R S_s = -77 \text{ J} (\text{mol K})^{-1}$ is calculated, which is close to that derived from thermochemistry (Eqs. (28) and (29)) [53]. For instance at 70°C , $\Delta_R S_g$ is equal to $-45.9 \text{ J} (\text{mol K})^{-1}$. Moreover, the Gibbs free enthalpy is also determined for the catalytic surface and gas-phase reaction (Eq. (30)). The results display very good accordance of both values in the whole temperature range implying a difference of ca. 5% only (Fig. 7). As a consequence, the model of the H_2 oxidation on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ is assessed to be thermodynamically consistent.

$$\Delta_R S_g(T) = \sum_{\substack{i=1 \\ i \neq j}}^n \nu_{ij} S_{g,i}(T) \quad (28)$$

$$S_{g,i}(T) = S_{g,i}(T_0) + \int_{T_0}^T \frac{c_{p,i}}{T} dT \quad (29)$$

$$\Delta_R G = \Delta_R H - T \times \Delta_R S \quad (30)$$

3.2.3. Kinetic modelling of the H_2 – O_2 – NO_x reaction

The kinetic model of the H_2 oxidation in excess of O_2 is extended by additionally considering the NO reduction to yield N_2 and N_2O . The resulting model includes 6 gaseous and 8 surface species. Based on the mechanism suggested in our recent study, exclusively showing the participation of NO chemisorbed on Pt [25] and in line with literature [3,16,30,47] the model of the H_2 – O_2 – NO_x reaction on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ implies the adsorption and desorption of NO (Eq. (31)) and N_2O (Eq. (35)), the formation of N^* by dissociation of NO^* (Eq. (32)) and the reaction of NO^* with H^* (Eq. (33)). Furthermore, N_2 is assumed to be formed by combination of two N^* species (Eq. (36)), while N_2O originates from the reaction of N^* with NO^* (Eq. (34)). For the reduction of the quantity of free kinetic parameters, our model accounts for the direct genesis of gaseous N_2 from two N^* species. This simplification is supposed to be justified, since molecular nitrogen is shown not to stick significantly on Pt surfaces above -173°C [54]. Also, it is reported that produced N_2 promptly

desorbs without any formation of stable equilibrated N_2 surface species [55].



The mechanism presented above follows the one proposed by Koop and Deutschmann [47]. Very recent work suggested that reduction of NO can also occur by the addition of H^* to form HNO and HNOH surface intermediates on the active Pt sites [6]. However, this catalytic route is not considered here. The rate expressions corresponding to the reaction mechanism (Eqs. (31)–(36)) are described by Eqs. (37)–(48). Eq. (40) supposes that the activation energy of the formation of NO^* from N^* and O^* linearly depends on the O^* coverage as expressed by the factor α_{16} (Eq. (40)). $E_{16}(0)$ is the activation energy at zero coverage [47]. Very similar approach is considered for the desorption of H_2 and O_2 (Eqs. (8) and (10)).

$$r_{13} = A_{13} \exp\left(-\frac{E_{13}}{RT}\right) c_{\text{NO}} \Theta_* \quad (37)$$

$$r_{14} = A_{14} \exp\left(-\frac{E_{14}}{RT}\right) \Theta_{\text{NO}} \quad (38)$$

$$r_{15} = A_{15} \exp\left(-\frac{E_{15}}{RT}\right) \Theta_{\text{NO}} \Theta_* \quad (39)$$

$$r_{16} = A_{16} \exp\left(-\frac{E_{16}(0) - \alpha_{16} \Theta_{\text{O}}}{RT}\right) \Theta_{\text{N}} \Theta_{\text{O}} \quad (40)$$

$$r_{17} = A_{17} \exp\left(-\frac{E_{17}}{RT}\right) \Theta_{\text{NO}} \Theta_{\text{H}} \quad (41)$$

$$r_{18} = A_{18} \exp\left(-\frac{E_{18}}{RT}\right) \Theta_{\text{OH}} \Theta_{\text{N}} \quad (42)$$

$$r_{19} = A_{19} \exp\left(-\frac{E_{19}}{RT}\right) \Theta_{\text{NO}} \Theta_{\text{N}} \quad (43)$$

$$r_{20} = A_{20} \exp\left(-\frac{E_{20}}{RT}\right) \Theta_{\text{N}_2\text{O}} \Theta_* \quad (44)$$

$$r_{21} = A_{21} \exp\left(-\frac{E_{21}}{RT}\right) c_{\text{N}_2\text{O}} \Theta_* \quad (45)$$

$$r_{22} = A_{22} \exp\left(-\frac{E_{22}}{RT}\right) \Theta_{\text{N}_2\text{O}} \quad (46)$$

$$r_{23} = A_{23} \exp\left(-\frac{E_{23}}{RT}\right) \Theta_{\text{N}}^2 \quad (47)$$

Table 2
Kinetic parameters of the model of the NO_x reactions on Pt/WO₃/ZrO₂.

Parameter	Value	Unit	Reference
A ₁₃	87.6	[m s ⁻¹]	Calculated ^a
E ₁₃	0	[kJ mol ⁻¹]	[47]
A ₁₄	5.7 × 10 ⁵	[mol (m ² s) ⁻¹]	Numerical fit
E ₁₄	72.4	[kJ mol ⁻¹]	Calculated ^b
A ₁₅	9.6	[mol (m ² s) ⁻¹]	Calculated ^b
E ₁₅	86.8	[kJ mol ⁻¹]	Calculated ^b
A ₁₆	4.7	[mol (m ² s) ⁻¹]	Numerical fit
E ₁₆ (0)	72.0	[kJ mol ⁻¹]	Numerical fit
α ₁₆	31.0	[kJ mol ⁻¹]	[47]
A ₁₇	7.4e + 6	[mol (m ² s) ⁻¹]	Numerical fit
E ₁₇	72.4	[kJ mol ⁻¹]	Numerical fit
A ₁₈	4.0 × 10 ⁷	[m s ⁻¹]	Calculated ^b
E ₁₈	147.4	[kJ mol ⁻¹]	Calculated ^b
A ₁₉	22.6	[mol (m ² s) ⁻¹]	Numerical fit
E ₁₉	43.8	[kJ mol ⁻¹]	Numerical fit
A ₂₀	6.8 × 10 ⁴	[mol (m ² s) ⁻¹]	Calculated ^b
E ₂₀	86.1	[kJ mol ⁻¹]	Calculated ^b
A ₂₁	2.1	[m s ⁻¹]	Calculated ^a
E ₂₁	10.8	[kJ mol ⁻¹]	Calculated ^b
A ₂₂	2.1 × 10 ³	[mol (m ² s) ⁻¹]	Numerical fit
E ₂₂	0.73	[kJ mol ⁻¹]	[47]
A ₂₃	8.7 × 10 ¹⁷	[mol (m ² s) ⁻¹]	Numerical fit
E ₂₃	163.0	[kJ mol ⁻¹]	Numerical fit
A ₂₄	2.3 × 10 ¹⁶	[m s ⁻¹]	Calculated ^b
E ₂₄	395.6	[kJ mol ⁻¹]	Calculated ^b

^a Calculated with Eq. (21).

^b Calculated from thermodynamic constraints.

$$r_{24} = A_{24} \exp\left(-\frac{E_{24}}{RT}\right) c_{N_2} \Theta_{*}^2 \quad (48)$$

The pre-exponential factors of the adsorption of NO (A₁₃) and N₂O (A₂₁) are calculated by using Eq. (21) with S⁰(NO)=0.85 and S⁰(N₂O)=0.025 [47], while taking 162.5 °C as the mean temperature. The adsorption of NO is considered to be inactivated (E₁₃ = 0 kJ mol⁻¹), whereas the adsorption of N₂O is supposed as a slightly activated process; the respective value for the activation energy E₂₁ = 10.8 kJ mol⁻¹ is derived from NASA polynomials [47] to ensure thermodynamic consistency. The activation energy of N₂O desorption (E₁₉) as well as α₁₆ are adopted from the literature [47]. The kinetic parameters A₁₄, A₁₆, E₁₆(0), A₁₇, E₁₇, A₁₉, E₁₉, A₂₂, A₂₃ and E₂₃ are numerically fitted, whereas E₁₄, A₁₅, E₁₅, A₁₈, E₁₈, A₂₀, E₂₀, A₂₄, E₂₄ are calculated from thermodynamic constraints [48] Table 2.

The fitting calculations are performed based on the mass balances of the gaseous and surface species as described for the H₂ oxidation, while using the rate Eqs. (37)–(48) for the NO_x chemistry. The model of the catalytic H₂–O₂ reaction is coupled into the balance of the surface species by introducing Θ_H, Θ_{OH}, Θ_{H₂O} and Θ_O. For the fitting procedure, the experimental run with 2000 vppm NO_x and 6000 vppm H₂ is taken, whereas the free parameters are numerically adjusted by using the experimental NO_x and N₂O data. The fitted NO and N₂O traces, calculated H₂O proportion and corresponding R² parameters are demonstrated in Fig. 8 showing satisfactorily agreement with the experimental data; only for water a slight shift for the light-off is observed. It should be pointed out that due to the relative small number of experimental points, the corresponding R² values range from 0.63 and 0.72. The kinetic parameters of the deNO_x reactions are summarised in Table 2.

In the numeric modelling, the activation energy of the NO desorption (E₁₄) is estimated to be 72.4 kJ mol⁻¹ being in good agreement with the literature (82 kJ mol⁻¹) [40,44]. Contrary, the activation energy of the N₂O* formation (E₁₉ = 43.8 kJ mol⁻¹) is clearly lower as referred to literature (ca. 90 kJ mol⁻¹) [43,47,56], whereas the activation energy of the production of N₂ (E₂₃ = 163 kJ mol⁻¹) is higher than the value published (130 kJ mol⁻¹) [52]. Although the energy barrier of the N₂ gen-

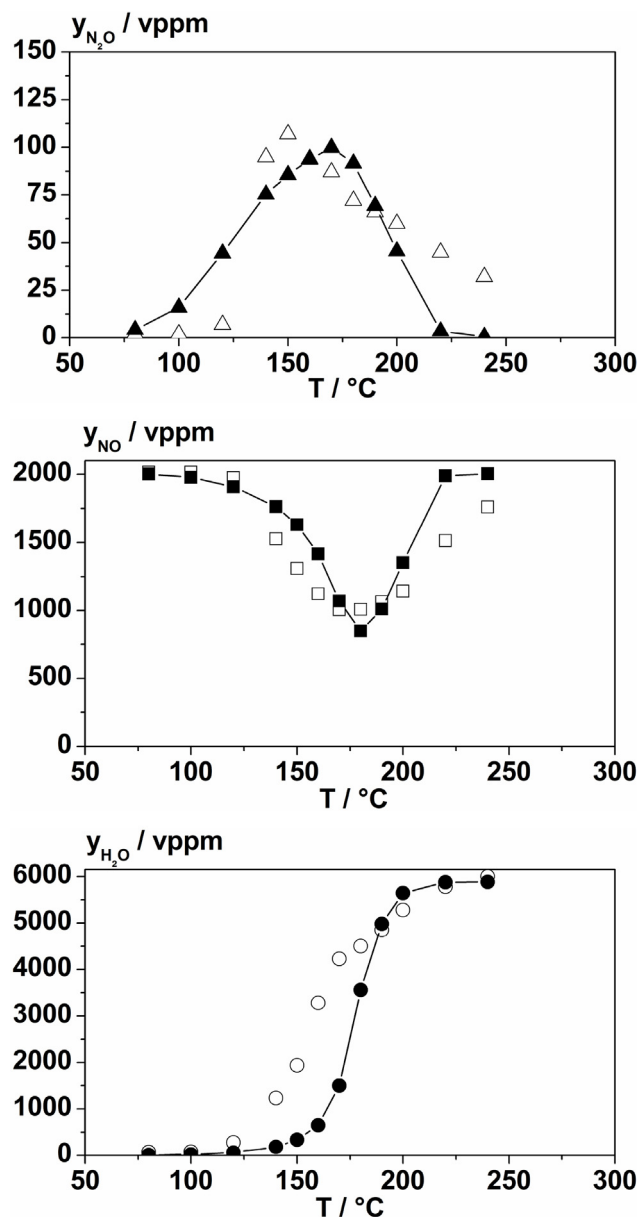


Fig. 8. Fractions of N₂O (Δ experimental, ▲ fitted), NO (□ experimental, ■ fitted) and H₂O (○ experimental, ● simulated) in H₂–O₂–NO_x reaction on Pt/WO₃/ZrO₂ (lines are guides for the eyes). Conditions: y(NO_x) = 2000 vppm, y(H₂) = 6000 vppm, y(O₂) = 6 vol%, N₂ balance, GHSV = 77,000 h⁻¹. R²(N₂O) = 0.63, R²(NO) = 0.72, R²(H₂O) = 0.67.

esis is high, this reaction step is still fast associated with the high frequency factor (A₂₃ = 8.7 · 10¹⁷ mol m⁻² s⁻¹). As a consequence, the production of gaseous N₂ occurs even faster than the nearly inactivated N₂O desorption (E₂₂ = 0.73 kJ mol⁻¹). Contrary, the dissociative adsorption of N₂ is supposed to be negligible due to its reasonably high activation energy (E₂₄ = 395.6 kJ mol⁻¹). Moreover, the activation energies of the dissociation of NO* (E₁₅ = 86.8 kJ mol⁻¹) and the recombination of N* with O* (E₁₆(0) = 72 kJ mol⁻¹) are lower as compared to literature indicating values above 100 kJ mol⁻¹ [43,47,52]. Also, the kinetic analysis indicates that the major path of the conversion of NO* is the dissociation (Eq. (32)) referring to the high coverage by NO*. In contrast to that, in lean H₂–deNO_x on Pt/BaO/Al₂O₃, it is discussed that NO* predominately reacts with adsorbed hydrogen according to Eq. (33) [52].

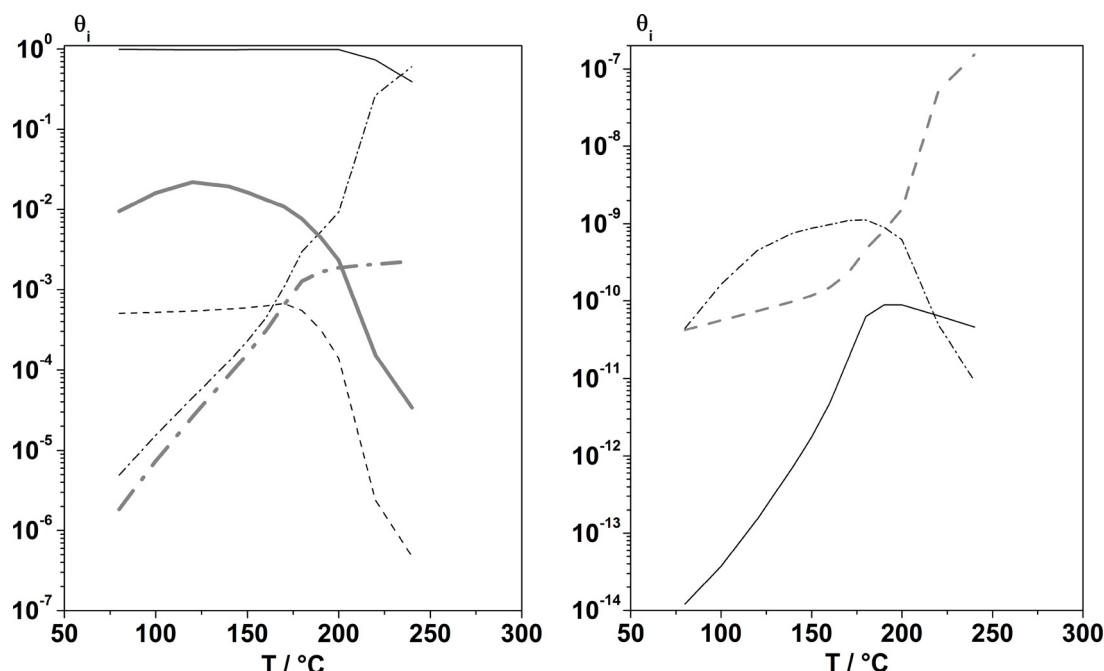


Fig. 9. Simulated coverages of Pt/WO₃/ZrO₂ in the H₂–O₂–NO_x reaction. Left: coverages by NO* (—), N* (---), H* (— · —), O* (·· ·) and free Pt site (— · · —); right: coverages by N₂O* (— · · ·), OH* (·· ·) and H₂O (—). Corresponding gas-phase fractions and conditions are demonstrated in Fig. 8.

Moreover, the modelling also provides simulation of the surface coverage suggesting predominant coverage of the Pt sites by NO at temperatures below 200 °C (Fig. 9). As a consequence, the low oxygen coverage is considered to explain the shift of the H₂ light-off to higher temperatures in the presence of NO. This light-off shift is observed to lie in the range of about 100 K, when NO is supplied. For example, the addition of NO to the feed shifts the H₂O light-off from a temperature below 50 °C (Fig. 2) to ca. 120 °C (Fig. 8 and Figs. 10–12). The relatively high NO surface coverage is in line with in situ DRIFTS studies of Pt/WO₃/ZrO₂ performed under very similar reaction conditions showing clear bands of NO coordinated to Pt sites [25]. Furthermore, the simulations indicate rapid decrease in the NO coverage above 200 °C changing the prevailing surface species towards O*. This probably occurs due to the acceleration of the combination of N* and O* to NO* as well as desorption of NO (backward reactions of Eqs. (31) and (32)), both yielding free adsorption sites for the adsorption of O₂. Additionally, the high coverage by NO below 150 °C substantiates the appreciable formation of the by-product N₂O at low temperatures, as N₂O is produced by the combination of NO* and N* (Eq. (34)). Hence, the surface concentration of NO obviously drives the rate of N₂O genesis, although N₂O is thermodynamically not favoured under the reaction conditions established (Fig. 1). However, from the analysis of the reaction rates we deduce that the N* species are mainly consumed by combination with another N* to form N₂ (Eq. (36)) and only to minor proportion by NO* yielding N₂O* (Eq. (34)). This interpretation substantiates the high N₂ selectivity of Pt/WO₃/ZrO₂ as compared to traditional Pt catalysts, e.g. Pt/Al₂O₃, forming N₂O as major product [25]. For instance, Pt/WO₃/ZrO₂ shows a N₂ selectivity of 90% (predicted: 84%) at maximum NO_x conversion, i.e. 160 °C (Fig. 8).

Pt/WO₃/ZrO₂ reveals lower energy barrier of the NO dissociation (86.8 kJ mol^{−1} vs. 108 kJ mol^{−1} for Pt/Al₂O₃ [47] and Pt/BaO/Al₂O₃ [52]); thus, increasing the coverage by N evoking N₂. It is suggested that the superior formation of N₂ on Pt/WO₃/ZrO₂ is associated with the increase of the electron density on the Pt sites by electronic interaction with the WO₃/ZrO₂ substrate as derived from a systematic DRIFTS study of Pt/WO₃/ZrO₂, Pt/ZrO₂ and Pt/Al₂O₃ using CO as probe molecule [25].

Another crucial feature of the H₂–O₂–NO_x reaction is the decrease in the NO_x conversion at higher temperatures (Fig. 8). This effect is related to the inclining coverage by O* above 200 °C (Fig. 9) drastically decreasing Θ_{NO} and Θ_{N} (Fig. 9) and suppressing the dissociation of NO* (Eq. (32)) as well as combination of N* (Eq. (36)). Further, the growth of the oxygen coverage leads to the acceleration of the production of H₂O. The kinetic analysis suggests that the formation of OH* (Eq. (3)) represents the rate-limiting step of the genesis of H₂O assigned to the low coverage of H*.

3.2.4. Validation of the kinetic model of the H₂–O₂–NO_x reaction

For validation of the kinetic model, simulations are conducted producing satisfactory prediction of the measured traces of NO_x, N₂O and H₂O as expressed by respective R^2 parameters (Figs. 10–12). As a noticeable feature, the model tends to predict slightly higher N₂O proportions. Exemplarily, for the feed containing 1000 vppm NO, 10,000 vppm H₂ and 6 vol% O₂, the simulation provides formation of 140 vppm N₂O ($S(\text{N}_2\text{O})=16\%$) at 150 °C, whereas the experiment shows 50 vppm only corresponding to a lower N₂O selectivity of 8% (Fig. 12). It should also be noted that below 150 °C, the formation of water is predicted to form slightly slower. The start of the modelled light-off is indicated at 150 °C, whereas in the experiment it is ca. 20 K lower. These deviations are mainly attributed to the lack of kinetic parameters referring to the present Pt/WO₃/ZrO₂ catalyst. Furthermore, the structure sensitivity of supported Pt catalysts in the H₂ deNO_x reaction [57] could also affect the kinetics, which was not considered here as a consequence of the mean field approach followed. The majority of kinetic parameters of the H₂–O₂–NO_x model had to be adopted from related Pt catalysts (29 from 51 parameters), which obviously exhibit specific activity and N₂ selectivity. Therefore, the appearing differences are assessed to be intrinsic to the kinetic parameters implemented into the model. Additionally, deviations may also refer to the mean field approximation considering equivalence of the Pt sites. It is known from the literature that the catalytic activity of Pt can depend on particle size [58] and crystalline orientation [59]. Moreover, the surface coverages obtained from the simulations closely resemble that shown in Fig. 9.

Table 3Reaction enthalpies and entropies of the NO_x reactions at 150 °C derived from thermo-chemical data and kinetic parameters of the catalytic surface model.

Overall reaction	$\Delta_R H / \text{kJ mol}^{-1}$		$\Delta_R S / \text{J (mol K)}^{-1}$	
	Gas-phase	Surface	Gas-phase	Surface
$\text{NO(g)} + \text{H}_2\text{(g)} \rightarrow 0.5 \text{N}_2\text{(g)} + \text{H}_2\text{O(g)}$	−334	−312	−61.4	−33.5
$\text{NO(g)} + 0.5 \text{H}_2\text{(g)} \rightarrow 0.5 \text{N}_2\text{O(g)} + 0.5 \text{H}_2\text{O(g)}$	−171	−161	−75.0	−65.2
$\text{N}_2\text{O(g)} + \text{H}_2\text{(g)} \rightarrow \text{N}_2\text{(g)} + \text{H}_2\text{O(g)}$	−325	−304	27.0	63.3

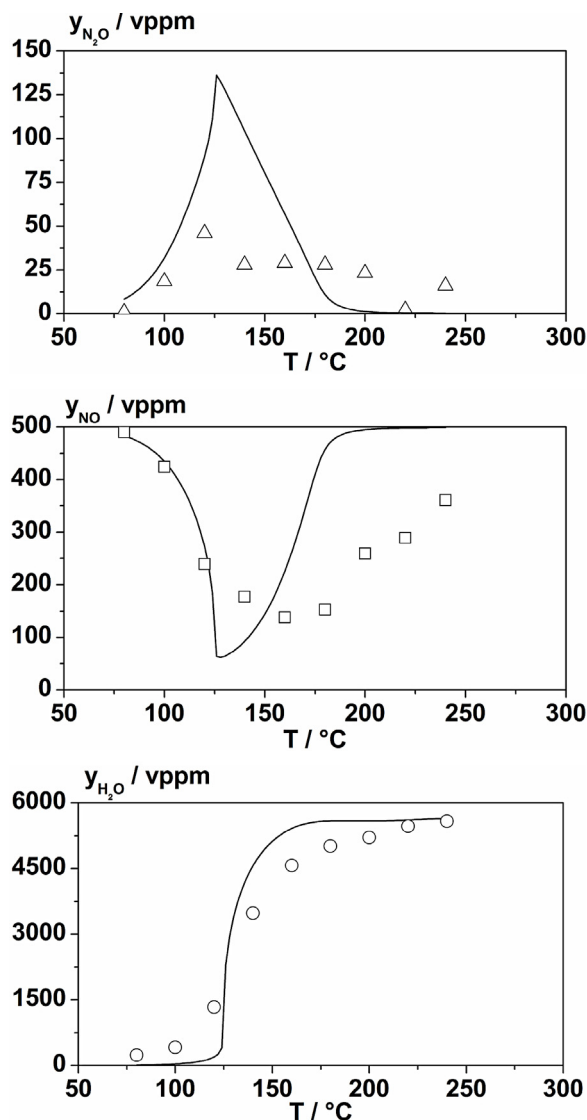


Fig. 10. Experimental fractions of N₂O (Δ), NO (□) and H₂O (○) and corresponding simulated fractions (—) in the H₂–O₂–NO_x reaction on Pt/WO₃/ZrO₂. Conditions: $y(\text{NO}_x) = 500$ vppm, $y(\text{H}_2) = 6000$ vppm, $y(\text{O}_2) = 6$ vol%, N₂ balance, GHSV = 77,000 h^{−1}. $R^2(\text{N}_2\text{O}) = -5.1$, $R^2(\text{NO}) = -0.87$, $R^2(\text{H}_2\text{O}) = 0.90$.

The thermodynamic consistency of the kinetic model of the H₂–O₂–NO_x reaction is checked as described in Section 3.2.2 (Eqs. (22) and (23)). For this purpose, the reaction enthalpy and entropy of the catalytic pathways are calculated implying the NO decomposition (Eqs. (49) and (50)), N₂O formation (Eqs. (51) and (52)) and N₂O decomposition (Eqs. (52) and (53)) and are compared with the thermo-chemical data of the corresponding gas-phase reactions (Eqs. (26) and (28)), i.e. $\text{NO(g)} + \text{H}_2\text{(g)} \rightarrow 0.5 \text{N}_2\text{(g)} + \text{H}_2\text{O(g)}$, $\text{NO(g)} + 0.5 \text{H}_2\text{(g)} \rightarrow 0.5 \text{N}_2\text{O(g)} + 0.5 \text{H}_2\text{O(g)}$ and $\text{N}_2\text{O(g)} + \text{H}_2\text{(g)} \rightarrow \text{N}_2\text{(g)} + \text{H}_2\text{O(g)}$. The results are demonstrated in Table 3 evidencing only less than 10% difference between the values of the surface and

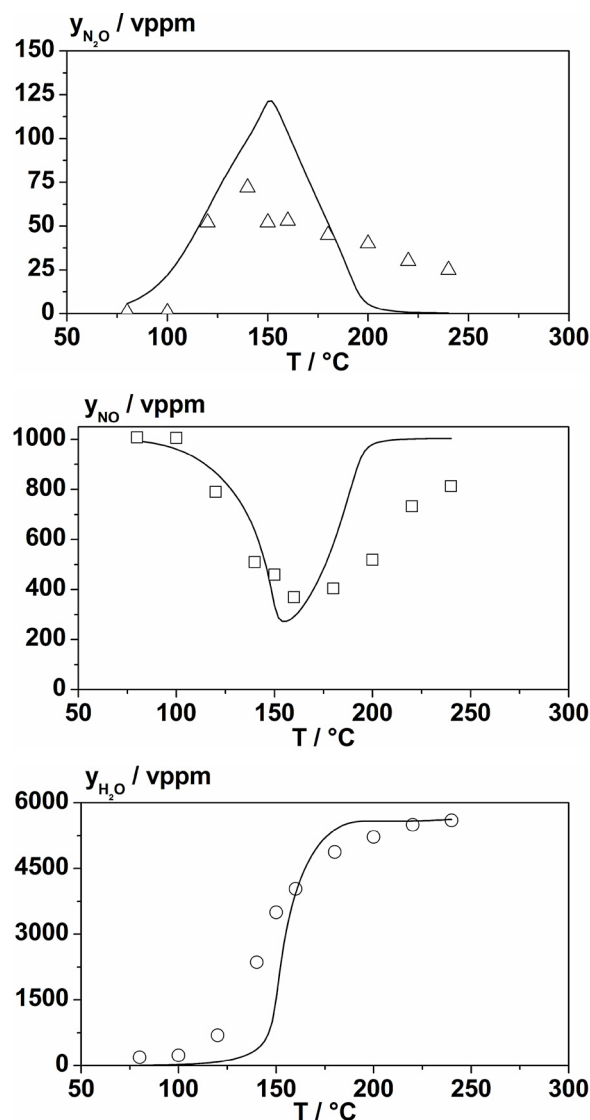


Fig. 11. Experimental fractions of N₂O (Δ), NO (□) and H₂O (○) and corresponding simulated fractions (—) in the H₂–O₂–NO_x reaction on Pt/WO₃/ZrO₂. Conditions: $y(\text{NO}_x) = 1000$ vppm, $y(\text{H}_2) = 6000$ vppm, $y(\text{O}_2) = 6$ vol%, N₂ balance, GHSV = 77,000 h^{−1}. $R^2(\text{N}_2\text{O}) = -1.4$, $R^2(\text{NO}) = 0.25$, $R^2(\text{H}_2\text{O}) = 0.80$.

gas-phase reactions. Furthermore, the Gibbs free enthalpy is evaluated for both pathways (Eq. (30)). Fig. 13 displays good agreement of the $\Delta_R G$ values of the gas-phase and catalytic surface reaction in the entire temperature regime. The relative difference is at most 5% only observed for the NO reduction to N₂O (80 °C), while for the NO reduction to N₂ it is 3.6% and for N₂O reduction 2.5%, respectively. Consequently, this comparison indicates thermodynamic accordance of the kinetic parameters. Furthermore, the used reaction mechanism (Eqs. (1)–(6) and (31)–(36)) with its respective kinetic parameters (Tables 1 and 2) is also consistent for the participation of O₂ in the NO reduction [22,60] as exemplarily expressed by

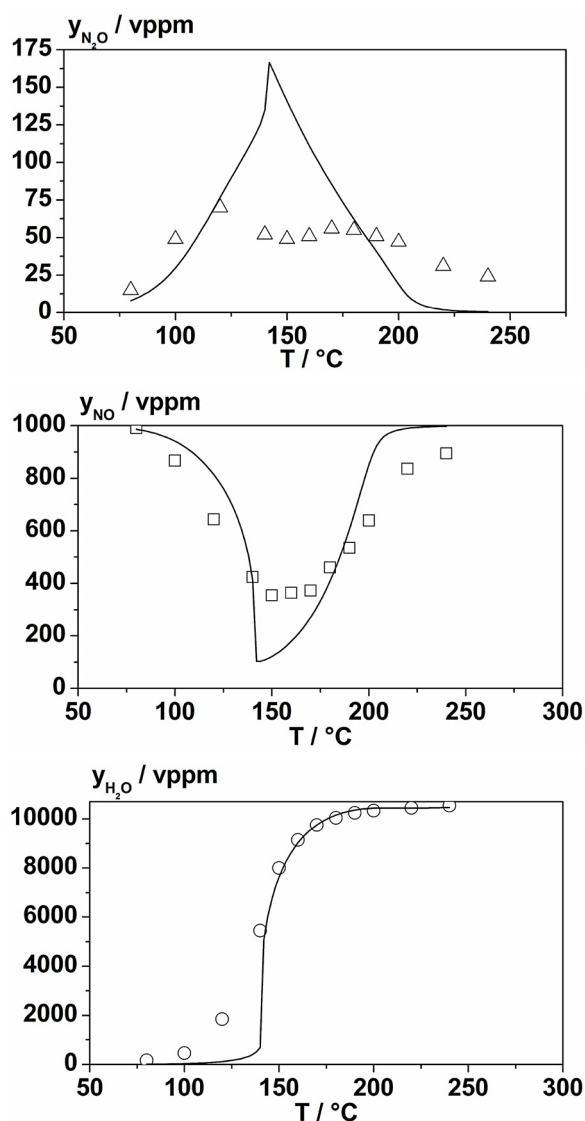


Fig. 12. Experimental fractions of N_2O (Δ), NO (\square) and H_2O (\circ) and corresponding simulated fractions (—) in the H_2 – O_2 – NO_x reaction on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$. Conditions: $y(\text{NO}_x)=1000$ vppm, $y(\text{H}_2)=10,000$ vppm, $y(\text{O}_2)=6$ vol%, N_2 balance, $\text{GHSV}=77,000\text{ h}^{-1}$. $R^2(\text{N}_2\text{O})=-7.9$, $R^2(\text{NO})=0.56$, $R^2(\text{H}_2\text{O})=0.86$.

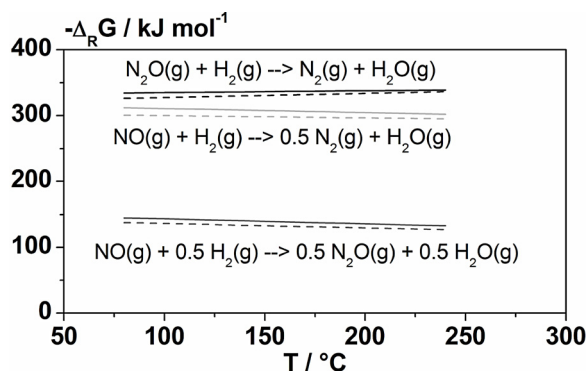


Fig. 13. Gibbs free enthalpy calculated with thermo-chemical data (solid lines) and kinetic parameters of the surface reaction on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ (dashed lines) for following conversions: $\text{NO}(\text{g}) + \text{H}_2(\text{g}) \rightarrow 0.5 \text{N}_2(\text{g}) + \text{H}_2\text{O}(\text{g})$ (—), $\text{NO}(\text{g}) + 0.5 \text{H}_2(\text{g}) \rightarrow 0.5 \text{N}_2\text{O}(\text{g}) + 0.5 \text{H}_2\text{O}(\text{g})$ (---) and $\text{N}_2\text{O}(\text{g}) + \text{H}_2(\text{g}) \rightarrow \text{N}_2(\text{g}) + \text{H}_2\text{O}(\text{g})$ (—).

the overall reaction $2 \text{NO}(\text{g}) + 3 \text{H}_2(\text{g}) + 0.5 \text{O}_2(\text{g}) \rightarrow \text{N}_2(\text{g}) + 3 \text{H}_2\text{O}(\text{g})$ (gas phase: $\Delta_R G(150^\circ\text{C}) = -838.1\text{ kJ mol}^{-1}$, surface reaction: $\Delta_R G(150^\circ\text{C}) = -796.7\text{ kJ mol}^{-1}$). This conversion is described as linear combination of above-mentioned elementary reactions.

$$\Delta_R H_s = E_1 - E_2(0) + E_5 - E_6 + E_7 - E_8 + E_{11} - E_{12} + E_{13} - E_{14} + E_{15} - E_{16}(0) + 0.5(E_{23} - E_{24}) \quad (49)$$

$$\Delta_R S_s = R \ln \left(\frac{A_1}{A_2} \frac{A_5}{A_6} \frac{A_7}{A_8} \frac{A_{11}}{A_{12}} \frac{A_{13}}{A_{14}} \frac{A_{15}}{A_{16}} \left(\frac{A_{23}}{A_{24}} \right)^{0.5} \right) \quad (50)$$

$$\Delta_R H_s = 0.5(E_1 - E_2(0) + E_5 - E_6 + E_7 - E_8 + E_{11} - E_{12}) + E_{13} - E_{14} + 0.5(E_{15} - E_{16}(0) + E_{19} - E_{20} + E_{22} - E_{21}) \quad (51)$$

$$\Delta_R H_s = R \ln \left(\left(\frac{A_1}{A_2} \frac{A_5}{A_6} \frac{A_7}{A_8} \frac{A_{11}}{A_{12}} \right)^{0.5} \frac{A_{13}}{A_{14}} \left(\frac{A_{15}}{A_{16}} \frac{A_{19}}{A_{20}} \frac{A_{22}}{A_{21}} \right)^{0.5} \right) \quad (52)$$

$$\Delta_R H_s = E_1 - E_2(0) + E_5 - E_6 + E_7 - E_8 + E_{11} - E_{12} + E_{15} - E_{16}(0) - E_{19} + E_{20} + E_{21} - E_{22} + E_{23} - E_{24} \quad (53)$$

$$\Delta_R S_s = R \ln \left(\frac{A_1}{A_2} \frac{A_5}{A_6} \frac{A_7}{A_8} \frac{A_{11}}{A_{12}} \frac{A_{15}}{A_{16}} \frac{A_{20}}{A_{19}} \frac{A_{21}}{A_{22}} \frac{A_{23}}{A_{24}} \right) \quad (54)$$

4. Conclusions

It was recently shown that $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ exhibits high low-temperature activity and pronounced N_2 selectivity in the NO_x reduction by H_2 under O_2 -rich conditions. For the advancement of the understanding of this reaction, we developed an elementary kinetic mean field model based on a systematic series of kinetic studies and a reaction mechanism suggested in the literature. The model included 6 gas-phase and 8 surface species forming a network of 48 forward and backward reactions. To reduce the number of free kinetic parameters, the catalytic H_2 – O_2 reaction was modelled independently and then the NO_x reduction implying the formation of N_2 and N_2O was implemented. Pre-exponential factors were estimated from kinetic gas theory and some kinetic parameters were adopted from the literature, while remaining parameters were obtained by numeric fitting. The constructed model of the H_2 – O_2 – NO_x reaction on $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ was useful to predict experiments and was found to reveal appropriate thermodynamic consistency showing the relevance of the kinetic model.

Finally, it should be stated that despite the good thermodynamic correspondence of the kinetic model, some differences of experiments and predictions remain. These deviations are partially referred to the mean field approach, which assumes all Pt sites to be equivalent. However, it should also be taken into consideration that a multitude of kinetic parameters had to be adopted from related Pt catalysts. Therefore, we suppose that the experimental evaluation of more kinetic parameters specific for $\text{Pt}/\text{WO}_3/\text{ZrO}_2$ might complement the model.

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